

# STRESS CONCENTRATION EXAMPLES

MET 4501

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## ROAD MAP FOR THE STRESS-LIFE METHOD – FULLY REVERSED SIMPLE LOADING

1. Determine  $S'_e$  either from test data or

$$S'_e = \begin{cases} 0.5S_{ut} & S_{ut} \leq 200 \text{ kpsi (1400 MPa)} \\ 100 \text{ kpsi} & S_{ut} > 200 \text{ kpsi} \\ 700 \text{ MPa} & S_{ut} > 1400 \text{ MPa} \end{cases} \quad (6-10)$$

2. Modify  $S'_e$  to determine  $S_e$ .

$$S_e = k_a k_b k_c k_d k_e S'_e \quad (6-17)$$

- a. Surface factor,  $k_a$

$$k_a = a S_{ut}^b \quad (6-18)$$

**Table 6–2** Curve Fit Parameters for Surface Factor, Equation (6–18)

Surface Finish	Factor $a$		Exponent $b$
	$S_{ut}$ , kpsi	$S_{ut}$ , MPa	
Ground	1.21	1.38	-0.067
Machined or cold-drawn	2.00	3.04	-0.217
Hot-rolled	11.0	38.6	-0.650
As-forged	12.7	54.9	-0.758

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### b. Size factor, $k_b$

**Rotating shaft.** For bending or torsion,

$$k_b = \begin{cases} (d/0.3)^{-0.107} = 0.879d^{-0.107} & 0.3 \leq d \leq 2 \text{ in} \\ 0.91d^{-0.157} & 2 < d \leq 10 \text{ in} \\ (d/7.62)^{-0.107} = 1.24d^{-0.107} & 7.62 \leq d \leq 51 \text{ mm} \\ 1.51d^{-0.157} & 51 < 254 \text{ mm} \end{cases} \quad (6-19)$$

For axial,

$$k_b = 1 \quad (6-20)$$

**Nonrotating member.** For bending, use Table 6–3 for  $d_e$  and substitute into Equation (6–19) for  $d$ .

### c. Load factor, $k_c$

$$k_c = \begin{cases} 1 & \text{bending} \\ 0.85 & \text{axial} \\ 0.59 & \text{torsion} \end{cases} \quad (6-25)$$

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### b. Temperature factor, $k_d$

$$\begin{aligned} S_T/S_{RT} &= 0.98 + 3.5(10^{-4})T_F - 6.3(10^{-7})T_F^2 \\ S_T/S_{RT} &= 0.99 + 5.9(10^{-4})T_C - 2.1(10^{-6})T_C^2 \end{aligned} \quad (6-26)$$

Either use the ultimate strength from Equation (6–26) to estimate  $S_e$  at the operating temperature, with  $k_d = 1$ , or use the known  $S_e$  at room temperature with  $k_d = S_T/S_{RT}$  from Equation (6–26).

### c. Reliability factor, $k_e$

**Table 6–4** Reliability Factor  $k_e$  Corresponding to 8 Percent Standard Deviation of the Endurance Limit

Reliability, %	Transformation Variate $z_a$	Reliability Factor $k_e$
50	0	1.000
90	1.288	0.897
95	1.645	0.868
99	2.326	0.814
99.9	3.091	0.753
99.99	3.719	0.702

## ROAD MAP FOR THE STRESS-LIFE METHOD – FULLY REVERSED SIMPLE LOADING

### 3. Determine fatigue stress-concentration factor, $K_f$ or $K_{fs}$ .

**3** Determine fatigue stress-concentration factor,  $K_f$  or  $K_{fs}$ . First, find  $K_t$  or  $K_{ts}$  from Table A-15.

$$K_f = 1 + q(K_t - 1) \quad \text{or} \quad K_{fs} = 1 + q_s(K_{ts} - 1) \quad (6-32)$$

Obtain  $q$  from either Figure 6-26 or 6-27.

Alternatively,

$$K_f = 1 + \frac{K_t - 1}{1 + \sqrt{a/r}} \quad (6-34)$$

Bending or axial:

$$\sqrt{a} = 0.246 - 3.08(10^{-3})S_{ut} + 1.51(10^{-5})S_{ut}^2 - 2.67(10^{-8})S_{ut}^3 \quad 50 \leq S_{ut} \leq 250 \text{ kpsi}$$

$$\sqrt{a} = 1.24 - 2.25(10^{-3})S_{ut} + 1.60(10^{-6})S_{ut}^2 - 4.11(10^{-10})S_{ut}^3 \quad 340 \leq S_{ut} \leq 1700 \text{ MPa} \quad (6-35)$$

Torsion:

$$\sqrt{a} = 0.190 - 2.51(10^{-3})S_{ut} + 1.35(10^{-5})S_{ut}^2 - 2.67(10^{-8})S_{ut}^3 \quad 50 \leq S_{ut} \leq 220 \text{ kpsi}$$

$$\sqrt{a} = 0.958 - 1.83(10^{-3})S_{ut} + 1.43(10^{-6})S_{ut}^2 - 4.11(10^{-10})S_{ut}^3 \quad 340 \leq S_{ut} \leq 1500 \text{ MPa} \quad (6-36)$$

## ROAD MAP FOR THE STRESS-LIFE METHOD – FULLY REVERSED SIMPLE LOADING

4. Apply  $K_f$  to the nominal completely reversed stress,  $\sigma_a = K_f \sigma_{a0}$ .
5. Determine  $f$  from Figure 6-23 or Equation (6-11). For  $S_{ut}$  lower than the range, use  $f = 0.9$ .

$$\begin{aligned} f &= 1.06 - 2.8(10^{-3})S_{ut} + 6.9(10^{-6})S_{ut}^2 & 70 < S_{ut} < 200 \text{ ksi} \\ f &= 1.06 - 4.1(10^{-4})S_{ut} + 1.5(10^{-7})S_{ut}^2 & 500 < S_{ut} < 1400 \text{ MPa} \end{aligned} \quad (6-11)$$

$$a = (f S_{ut})^2 / S_e \quad (6-13)$$

$$b = -[\log(f S_{ut}/S_e)]/3 \quad (6-14)$$

6. Determine fatigue strength  $S_f$  at  $N$  cycles, or,  $N$  cycles to failure at a reversing stress  $\sigma_{ar}$ .

(Note: This only applies to purely reversing stresses where  $\sigma_m = 0$ .)

$$S_f = aN^b \quad (6-12)$$

$$N = (\sigma_{ar}/a)^{1/b} \quad (6-15)$$

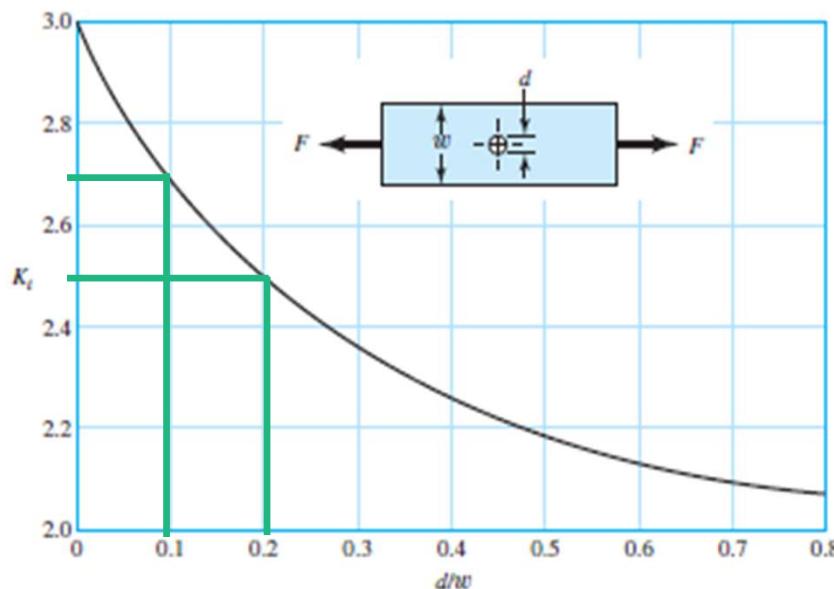
## EXAMPLE 1

**Table A-15**

Charts of Theoretical Stress-Concentration Factors  $K_t^*$

**Figure A-15-1**

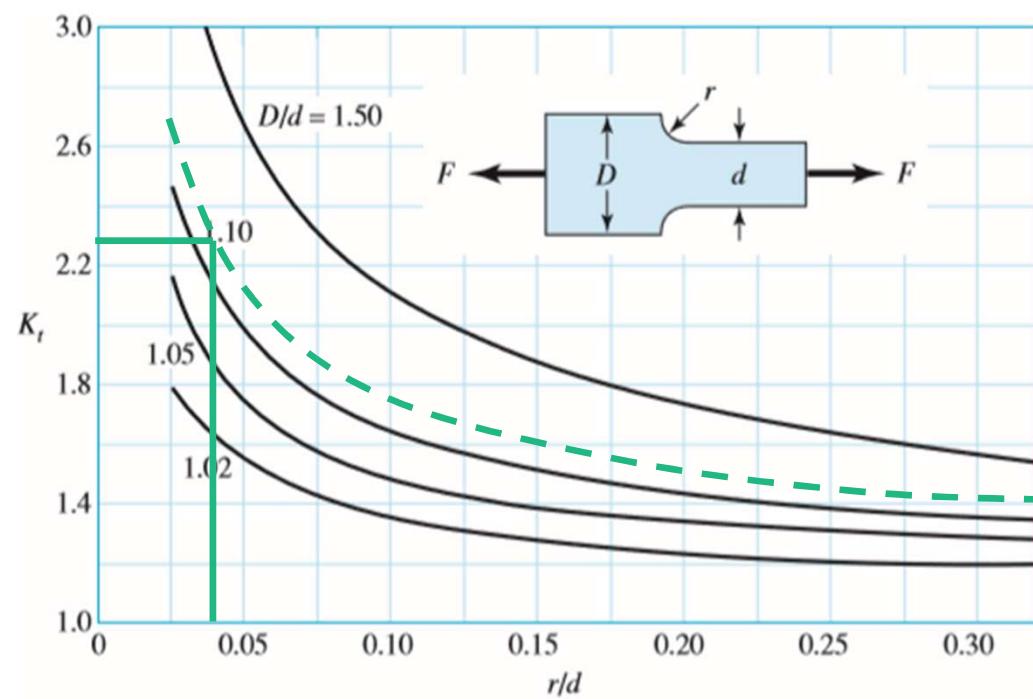
Bar in tension or simple compression with a transverse hole.  $\sigma_0 = F/A$ , where  $A = (w - d)t$  and  $t$  is the thickness.



## EXAMPLE 1

**Figure A-15-5**

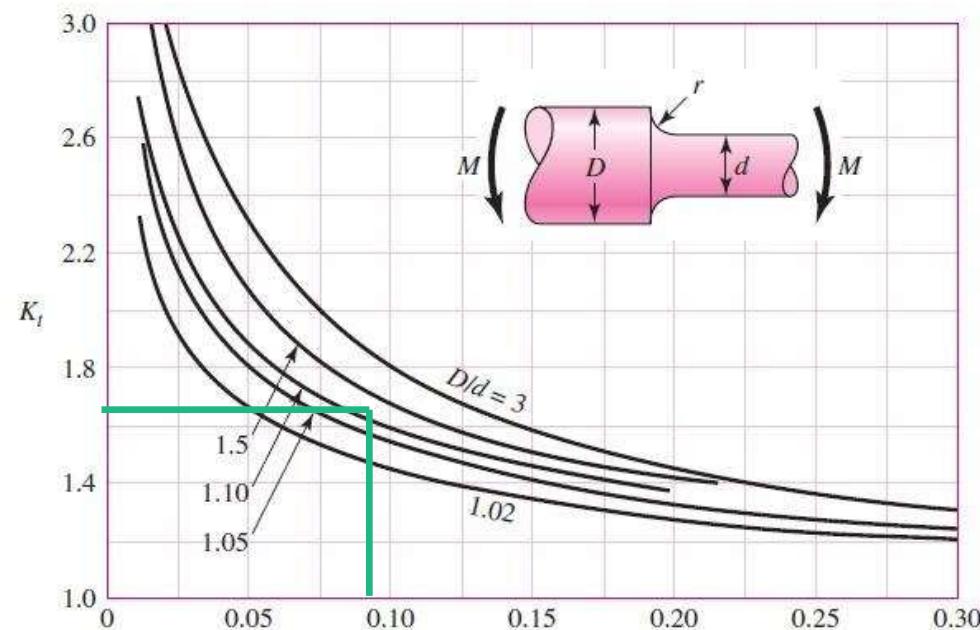
Rectangular filleted bar in tension or simple compression.  
 $\sigma_0 = F/A$ , where  $A = dt$  and  
t is the thickness.



## EXAMPLE 2

**Figure A-15-9**

Round shaft with shoulder fillet in bending.  $\sigma_0 = Mc/I$ , where  $c = d/2$  and  $I = \pi d^4/64$ .



## EXAMPLE 2

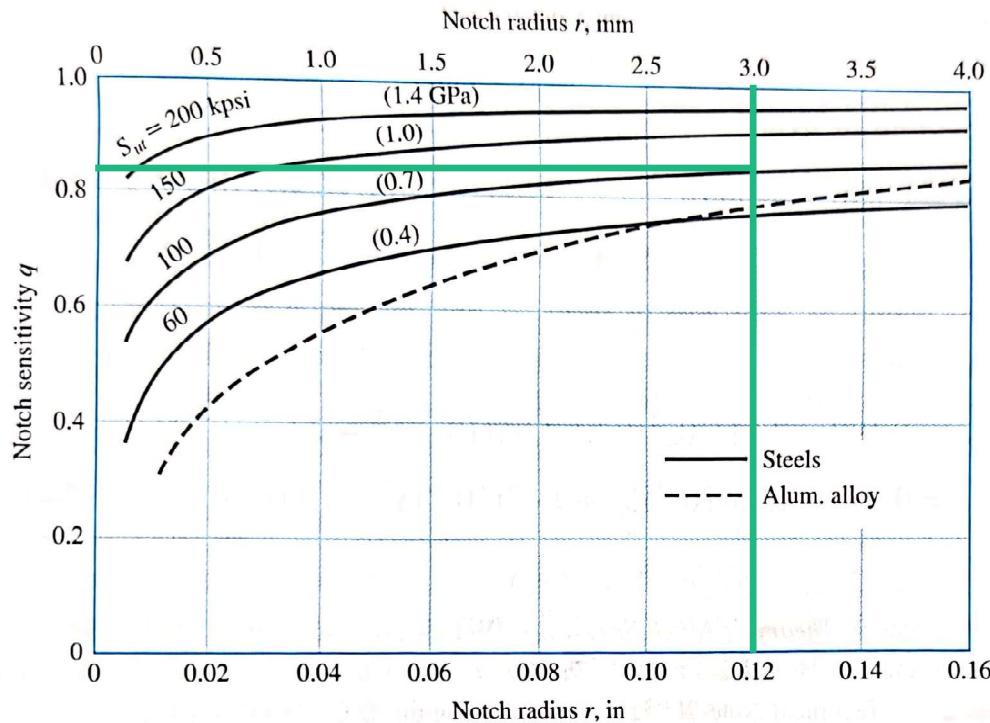


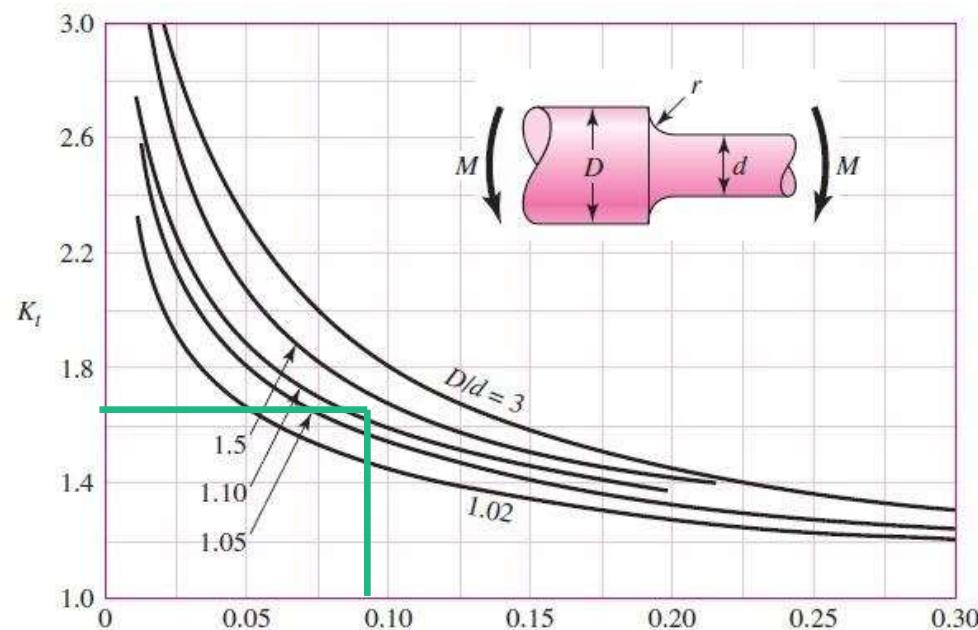
Figure 6–26

Notch-sensitivity charts for steels and UNS A92024-T wrought aluminum alloys subjected to reversed bending or reversed axial loads. For larger notch radii, use the values of  $q$  corresponding to the  $r = 0.16$ -in (4-mm) ordinate. Source: Sines, George and Waisman, J. L. (eds.), *Metal Fatigue*, McGraw-Hill, New York, 1969.

### EXAMPLE 3

**Figure A-15-9**

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### EXAMPLE 3

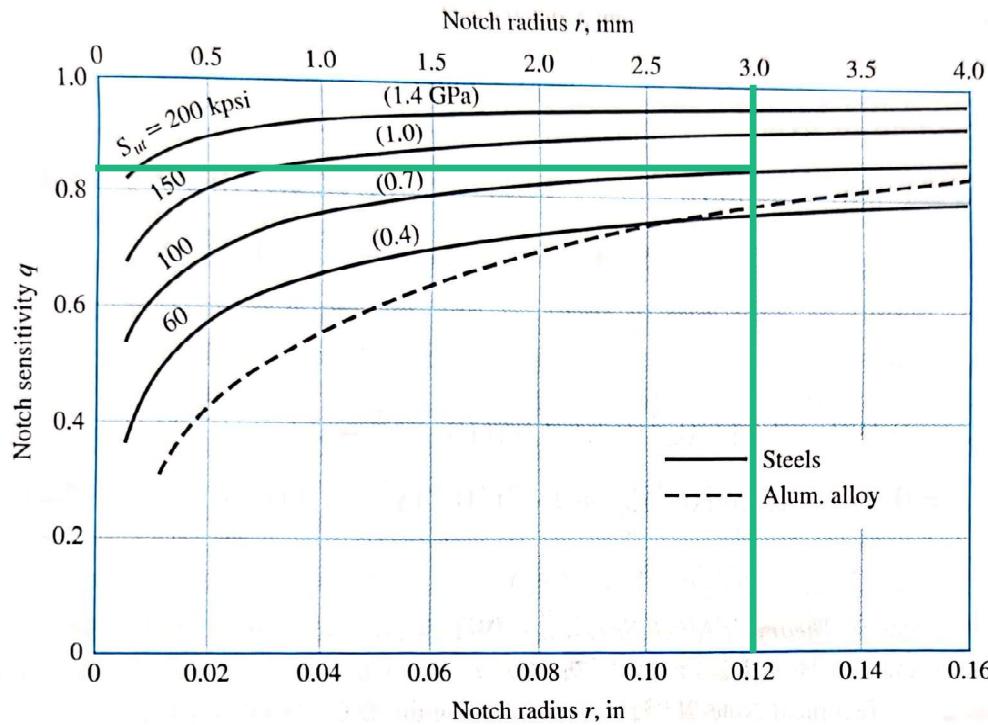


Figure 6–26

Notch-sensitivity charts for steels and UNS A92024-T wrought aluminum alloys subjected to reversed bending or reversed axial loads. For larger notch radii, use the values of  $q$  corresponding to the  $r = 0.16$ -in (4-mm) ordinate. Source: Sines, George and Waisman, J. L. (eds.), *Metal Fatigue*, McGraw-Hill, New York, 1969.